

Macro and micro prudential policies: sweet and lowdown in a credit network agent based model

Ermanno Catullo* Federico Giri[†] Mauro Gallegati [‡]

Abstract

The paper presents an agent based model reproducing a stylized credit network that evolves endogenously through the individual choices of firms and banks. We introduce in this framework a financial stability authority in order to test the effects of different prudential policy measures designed to improve the resilience of the economic system. Simulations show that combining micro and macro prudential policies reduces systemic risk, but at the cost of increasing bank capital volatility. Moreover, agent based methodology allows us to implement an alternative *meso* regulatory framework that take into consideration the connections between firms and banks. This policy targets only the more connected banks, increasing their capital requirement in order to reduce the diffusion of local shocks. Our results support the idea that the meso prudential policy is able to reduce systemic risk without affecting the stability of banks' capital structure.

Keywords: Micro prudential policy; Macro prudential policy; Credit Network; Meso prudential policy; Agent based model;

JEL classification codes: E50; E58; G18; G28; C63.

1 Introduction

The aim of this paper is to provide some insights into the interrelations between micro and macro prudential policies, the potential conflicts among them and to propose an alternative regulation framework based on the credit network topology, that we define as the meso prudential policy. For this purpose, we build an agent based model including a credit network where banks and firms can have multiple relation lending. We use this model to answer two different questions: a) are there any drawbacks when the financial stability authority uses a combination of micro and macro prudential policies to achieve its target? b) Does a prudential policy that takes into account also

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24 the credit network relationships works better in terms of output and credit stabilization than the
25 one based on traditional micro/macro framework?

26 After the 2007/2008 financial crisis, the design and enforcement of effective prudential policies
27 aiming at preventing or reducing the effects of financial and credit crises became central in the
28 economic and political debate. According to Hanson et al. (2011) and Galati and Moessner (2013),
29 the micro and macro approaches to financial regulation differ in a fundamental way: micro policies
30 aims at reducing the riskiness of single financial institution, on the other hand macro prudential
31 policies are focused on mitigating the systemic effects of individual imbalances. While micro
32 prudential policy has a long tradition and has been extensively analyzed during the decades (see
33 Gorton and Winton, 2003, for a review), it was only in the aftermath of the Great Recession that
34 macro prudential policy captured the attention of economists. Despite the progress, Galati and
35 Moessner (2017) concludes that there is no general consensus about the effectiveness of macro
36 prudential policy as an instrument to reduce systemic risk.

37 A natural step forward in this research agenda would be the investigation of the combine effect
38 of micro and macro prudential measures. In fact, in different circumstances, micro and macro
39 prudential policy objectives may diverge (Angelini et al., 2012, Alessandri and Panetta, 2015, and
40 Osinski et al., 2013). For instance, during downturns, macro prudential policies may be oriented at
41 softening banks patrimonial requirement in order to avoid a credit crunch. On the contrary, micro
42 prudential policy may aim at consolidating the financial position of banks enhancing the capital
43 requirements. This conflictive dichotomy is the subject of our research.

44 In order to answer our research questions, we build an agent based model that includes a
45 simplified credit network among firms and banks evolving endogenously according to the individual
46 supply and demand of loans. Agent based models (henceforth ABM, see Delli Gatti et al., 2005
47 and Tesfatsion and Judd, 2006, for a detailed description) have become popular among economists
48 as an alternative tool with respect to standard DSGE models. In the context of micro/macro
49 prudential policy interaction, the choice of setting up an ABM is motivated by the fact that such
50 kind of models are particularly suited to describe, in a unified framework, individual agent behavior
51 and macroeconomic patterns.

52 Several recent contributions tried to investigate financial instability in a macro ABM model.
53 Cincotti et al. (2012) finds that the dynamic adjustment of capital requirements performs better in
54 terms of output stabilization with respect to fixed ones. Likewise, Baptista et al. (2016) explores the
55 effects of a loan-to-income policy finding that such policy may successfully smooth the house price
56 cycle. Assenza et al. (2017) compares two different macroprudential policies, capital requirement
57 and liquidity constraints, analyzing the differences on the dynamic of the system. The adjustment
58 of the capital requirement results to be more effective than liquidity ratios to reduce the probability
59 of a crisis. Popoyan et al. (2017) builds an ABM model with heterogeneous banks and firms in order
60 to test the effectiveness of different macro prudential policies finding that imposing a minimum

61 capital requirement and counter-cyclical capital buffer is the policy that best resemble the Basel
62 III regulatory framework in a much more simplified way. However, in a similar set up, Krug et al.
63 (2014) finds that the macro prudential policy overlays impact with micro prudential measures has
64 a very limited impact on financial stability. Moreover, Riccetti et al. (2017) finds that a tight
65 regulation can generate a contraction of the credit supply whereas loose financial regulation can
66 generate financial instability.

67 The following results emerge from our investigation: *a)* the combination of micro and macro
68 prudential policy reduces instability and the probability of an economic crisis with respect to the
69 scenario that implements the micro prudential policy only, *b)* However, such instability does not
70 disappear but it is transmitted to the banking system through the higher volatility of banks' equity.
71 *c)* The implementation of a meso prudential policy is effective in reducing systemic risk through
72 tightening the capital requirements of more connected banks only. Exploiting network topology, it
73 is possible to better coordinate micro and macro prudential policy in order to increase the resilience
74 of the economic system without impacting on the performance of the banking system.

75 The paper is organized as follow: Section 2 presents the model; Section 3 describes the mi-
76 cro/macro prudential policy experiments; Section 4 introduces the the meso prudential policy
77 experiment. Finally, Section 5 concludes.

78 2 The Model

79 Our model economy reproduces a simplified credit network that evolves endogenously (Riccetti
80 et al., 2013, Catullo et al., 2015, Catullo et al., 2017). The credit market is populated by M banks
81 and N heterogeneous firms. Banks provide credit to firms that produce an homogeneous final
82 good. Both firms and banks are bounded rational agents and they are profit maximizers choosing
83 their desired level of leverage. The size of their balance sheet determines their expected profits and
84 the related default risk they have to bear. Indeed, bank credit supply and firm demand derive from
85 the leverage choices of the agents that, consequently, shape the evolution of the credit network.

86 2.1 Banks

87 In every period, banks determine their credit supply and the interest rate on loans. Each bank b
88 gradually adjusts credit supply with respect to the loan demand received in the previous period
89 ($L_{b,t-1}^D$). Moreover, banks have to comply with the capital requirement fixed by the financial
90 stability authority (ν_t). The associated maximum loan supply would be equal to ($L_{bt}^\nu = E_{bt}/\nu$).
91 Therefore, bank's desired loan supply is equal to the minimum between loan previously demand
92 ($L_{b,t-1}^D$) and the maximum loan supply authorized by the financial stability authority (L_{bt}^ν):

$$L_{bt}^O = \min(L_{b,t-1}^D, L_{bt}^\nu). \quad (1)$$

93 We assume that banks adapt gradually their credit supply (L_{bt}^S) to the desired offer (L_{bt}^O), thus:

$$L_{bt}^S = \begin{cases} L_{bt}^O & \text{if } L_{b,t-1}^S(1-\delta) \leq L_{b,t-1}^O \leq L_{b,t-1}^S(1+\delta) \\ L_{bt}^S(1-\delta) & \text{if } L_{b,t-1}^O < L_{b,t-1}^S(1-\delta) \\ L_{bt}^S(1+\delta) & \text{if } L_{b,t-1}^O > L_{b,t-1}^S(1+\delta). \end{cases} \quad (2)$$

94 Moreover, banks may provide a maximum amount of their supply to a single firm (L_{ibt}^{SM}):

$$L_{ibt}^{SM} = \zeta L_{bt}^S. \quad (3)$$

95 Deposits are computed residually as difference between loan supply and bank net-worth:

$$D_{bt} = L_{b,t}^S - E_{bt}, \quad (4)$$

96 assuming that the minimum loan supplied is equal to the bank net-worth.

97 Interest rate is computed in two steps. Firstly, following Gerali et al. (2010), banks maximize
98 expected profits establishing a relation between interest rate and bank leverage. Since deviations
99 from capital requirement are costly for the bank, they are charged directly on credit interest rates:

$$R_{bt} = \begin{cases} \eta r_t^d - k (E_{bt}/L_{bt}^S - \nu) (E_{bt}/L_{bt}^S)^2 & \text{if } E_{bt}/L_{bt}^S < \nu \\ \eta r_t^d & \text{if } E_{bt}/L_{bt}^S \geq \nu, \end{cases} \quad (5)$$

100 where the term $E_{bt}/L_{bt}^S < \nu$ captures the micro prudential policy intervention. Furthermore,
101 similar in spirit to the financial accelerator mechanism of Bernanke et al. (1999), banks fix a firm
102 specific interest rate premium (depending on firm's leverage (K_{it}^d/E_{it})) charging the following
103 interest rate to firms:

$$r_{ibt} = \bar{r} \left(\frac{E_{it}}{K_{it}^d} \right)^{-\beta} + R_{bt}. \quad (6)$$

104 Therefore, bank's profit (π_{bt}), obtained from the interest charged on loans allocated to firms J
105 after subtracting the bad debt (BD_{bt}) and capital costs, is:

$$\pi_{bt} = \sum_j^J r_{jbt} L_{jbt} - BD_{bt} - r_d D_{bt} - F. \quad (7)$$

106 Only a fraction of profits is accumulated by the banks, increasing their net worth ($E_{b,t+1}$),
107 indeed in line with the gradual adjusting processes that characterized the model we assume that
108 the larger is profit the higher are dividends, thus the net profit π_{bt}^N is equal to $\min(\pi_{bt}, \pi_{bt}^\gamma)$ with
109 $0 < \gamma < 1$.

$$E_{b,t+1} = E_{bt} + \pi_{bt}^N. \quad (8)$$

110 2.2 Firms

111 Firms use capital (K_{it}) to produce output using a linear production function:

$$Y_{it} = \phi K_{it}. \quad (9)$$

112 The firm's balance sheet is:

$$K_{it} = L_{it} + E_{it}. \quad (10)$$

113 Capital is given by the sum of the net-worth (E_{it}) and loans contracted at time t (L_{it}). Firms
114 can receive loans from more than one bank, thus the amount of loan borrowed by a firm is given
115 by the sum of the loans received by the set of lending banks (Z):

$$L_{it} = \sum_{z \in Z} L_{izt}. \quad (11)$$

116 Profits derive from revenues ($p_{it}\phi K_{it}$) minus a variable cost on production (cK_{it}) interests on
117 loans ($r_{it}L_{it}$) and a fixed cost (F), p_{it} is extracted from a uniform distribution ($p_{it} \sim U[0, 2]$)

$$\pi_{it} = p_{it}\phi K_{it} - r_{it}L_{it} - cK_{it} - F \quad (12)$$

118 Firms choose the desired level of production assuming that they would ask for loans only if
119 they do not have sufficient internal resources. Loan demanded (L_{it}^d) is equal to desired level of
120 capital (K_{it}) minus firm's net-worth $L_{it}^d = K_{it} - E_{it}$. Thus, if $K_{it} > E_{it}$:

$$E(\pi_{it}) = E(p)\phi K_{it} - \left(\bar{r} \frac{K_{it}^\beta}{E_{it}} + E(R_{bt}) \right) (K_{it} - E_{it}) - cK_{it} - F, \quad (13)$$

121 assuming that $E(R_{bt}) = R_{b,t-1}$, thus maximizing expected profit for K_{it} , the first order condition
122 is:

$$E(p)\phi - \bar{r}(\beta + 1) \frac{K_{it}^\beta}{E_{it}^\beta} + \bar{r} - R_{b,t-1} - c = 0. \quad (14)$$

123 If $K_{it} > E_{it}$ and $E(p)\phi - c - R_{b,t-1} + \bar{r} > 0$ the optimum capital level (K_{it}^O) is equal to:

$$K_{it}^O = \begin{cases} \frac{1}{(1+\beta)\bar{r}} (E(p)\phi - c - R_{b,t-1} + \bar{r})^{\frac{1}{\beta}} E_{it}, & \text{if } K_{it} > E_{it} \\ E_{it}, & \text{if } K_{it} \leq E_{it} \end{cases} \quad (15)$$

124 However, firms may adapt only gradually to their optimum quantity (K_{it}^O), thus the productive
125 quantity of capital (K_{it}^D) is computed as:

$$K_{it}^D = \begin{cases} \max(K_{it}^O, K_{i,t-1}^D * (1 - \delta)) & \text{if } K_{i,t-1}^D > K_{it}^O \\ \min(K_{it}^O, K_{i,t-1}^D * (1 + \delta)) & \text{if } K_{i,t-1}^D \leq K_{it}^O. \end{cases} \quad (16)$$

126 Therefore, if the capital desired (K_{it}^D) is greater than the firm net-worth (E_{it}), loan demand is
 127 equal to:

$$L_{it}^D = \min(K_{it}^D, K_{it}^O). \quad (17)$$

128 The quantity of capital effectively used in production depends on the quantity of loan effectively
 129 received L_{it} and thus is equal to:

$$K_{it}^E = L_{it} + E_{it}. \quad (18)$$

130 Similarly to the banking sector, only a fraction of the profits is accumulated by firms. Thus
 131 the net profit π_{it}^N is equal to $\min(\pi_{it}, \pi_{it}^\gamma)$ with $0 < \gamma < 1$.

$$E_{i,t+1} = E_{it} + \pi_{it}^N \quad (19)$$

132 2.3 Credit Matching

133 In each period, firms can receive credit from different banks. The matching process between credit
 134 demand and supply follows three steps. Firstly, firms, in a random order, apply for a loan to banks
 135 that provided credit to them in the previous period until their demand is fulfilled. Secondly, if firms
 136 do not receive enough credit, they ask for loans to banks that did not allocate all their supply in
 137 the previous step. Moreover, firms that did not receive credit in the previous period ask for loans
 138 to banks that still offer credit. In the third step, each firm that found lending banks in the previous
 139 periods may change the credit line in favor of another bank that offers better credit conditions
 140 both in terms of the amount of loan provided and the interest rate.

141 Following Delli Gatti et al. (2010) and Riccetti et al. (2014), each firm can change a randomly
 142 chosen linked bank with a new randomly chosen bank that has an excess of credit supply. Firms
 143 choose to remain linked with the previous bank or to shift to the new bank with a probability
 144 (Ps), that depends on the interest rate charged by the old and the new bank (respectively r_{new}
 145 and r_{old}) and the quantity of credit supplied to the firm (respectively L_{new}^s and L_{old}^s), with both
 146 of them not exceeding the loan demanded by the firm:

$$Ps = \max[Ps(r), Ps(L)], \quad (20)$$

147 where $Ps(r)$ and $Ps(L)$ are given by:

$$Ps(r) = \begin{cases} 1 - e^{(r_{new} - r_{old})/r_{new}} & \text{if } r_{new} < r_{old} \\ 0 & \text{otherwise} \end{cases} \quad (21)$$

$$P_s(L) = \begin{cases} 1 - e^{(L_{old}^s - L_{new}^s)/L_{new}^s} & \text{if } L_{new}^s > L_{old}^s \\ 0 & \text{otherwise} \end{cases} \quad (22)$$

148 thus, if the new bank offers lower interest rate and a larger amount of credit the probability
 149 that the firm will substitute the old bank with the new one increases.

150 2.4 Exit and Enter

151 Firms and bank with net-worth lower than zero exit from the economy and they are substituted
 152 by an equal number of agents, so the total number of agent is constant. The net-worth of the new
 153 enter firm (E_{it}) is equal to

$$E_{it} = \max[E_{Ft}^{med}, E_F^0], \quad (23)$$

154 where E_{Ft}^{med} is the median firm net-worth and E_F^0 a given minimum firm net-worth level.

155 Similarly, the net-worth of the new enter bank (E_{bt}) is equal to

$$E_{bt} = \max[E_{Bt}^{med}, E_B^0], \quad (24)$$

156 where E_{Bt}^{med} is the median bank net-worth and E_B^0 a given minimum bank net-worth level.

157 2.5 Simulation Time-Schedule

158 The simulation model follows a discrete agents' decision process divided in steps:

- 159 1. Banks offer credit
- 160 2. Firms determine loan demand
- 161 3. Credit matching among firms and banks
- 162 4. Firms and banks compute profit and net-worth
- 163 5. Failing firms and banks exit the market and new agents enter

164 when all this steps are implemented a new cycle of the computation starts again.

165 3 Simulation Results: Micro and Macro Prudential Policies

166 The simulated economy is populated by 1000 firms and 100 banks, simulations last for 1000 periods,
 167 discarding the first 500 as transient. We calibrated the model parameters aiming at reproducing
 168 realistic values of the output standard deviation and of the aggregate credit over output value. For
 169 a detailed explanation of the calibration exercise see Appendix A.

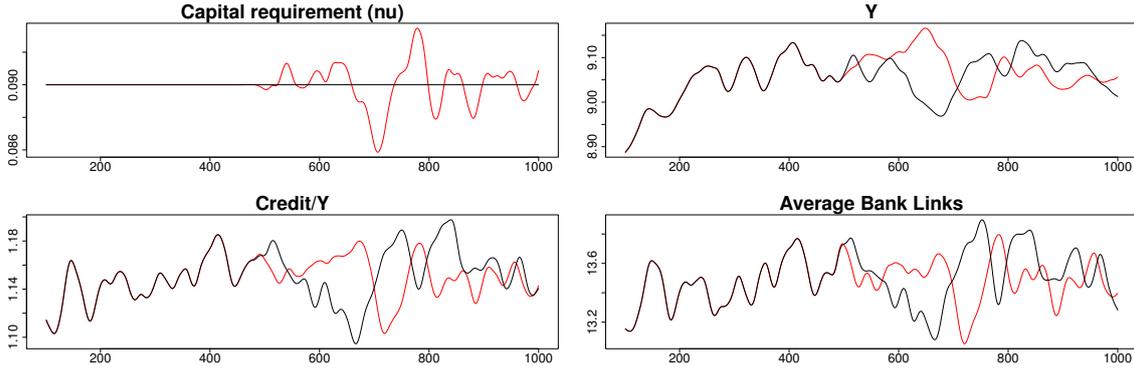


Figure 1: In black the baseline micro prudential scenario, in red the macro prudential scenario with $\chi = 0.8$. In all the figures, time on the x axis. In the top left figure, the capital requirement variation that are fixed in the baseline scenario while it fluctuate with the macro prudential policy. In the top right figure, the output time series. In the bottom left figure, aggregate credit over output variations. In the bottom right, the average number of firms at which each bank lend money.

170 In the baseline scenario, we only implement a micro prudential framework: according to Equa-
 171 tion (1) and (4) each bank have to adjust its leverage in order to satisfy the capital requirement
 172 (ν). Equation (1) governs the leverage dynamics, whereas Equation (4) drives the spread between
 173 the interest rates on deposits and wholesale credit. We compare the baseline micro prudential
 174 framework with a scenario where, in addition, a macro prudential policy is implemented as a time-
 175 varying capital requirement mechanism, similar in spirit to the one proposed by Angelini et al.
 176 (2014):

$$\nu_t = (1 - \rho)\bar{\nu} + \chi(1 - \rho)\Delta L_t/L_{t-1} + \rho\nu_t. \quad (25)$$

177 The parameter χ represents the strength of the macro prudential policy intervention. Assuming
 178 $\chi > 0$, the macro prudential authority behaves countercyclically, increasing ν_t when the aggregate
 179 amount of credit allocated in the economy (L_t) grows, and viceversa when credit decreases. When
 180 χ is negative the macro prudential policy is procyclical.

181 We apply the macro prudential policy after the period 500. Figure 1 shows that after the
 182 period 500 ν_t starts to change and this implies that the macro and micro dynamics of the model
 183 are affected by the intervention of the financial stability authority. We report the time series of
 184 output, credit over output and the average number of credit agreements of each bank, these last
 185 intended as links of the credit network.

186 Since results crucially depend on the value of χ , we perform a sensitivity analysis varying
 187 this parameter, considering 100 Monte Carlo simulations for each specification. We focused on
 188 the variations of the standard deviation of both credit and output, which give us a measure of
 189 the volatility of the system, and the crisis probability of credit and output provide a synthetic
 190 indicator of the vulnerability of the economy, this last measured as the frequency of a reduction
 191 lower than the -0.02 per cent.

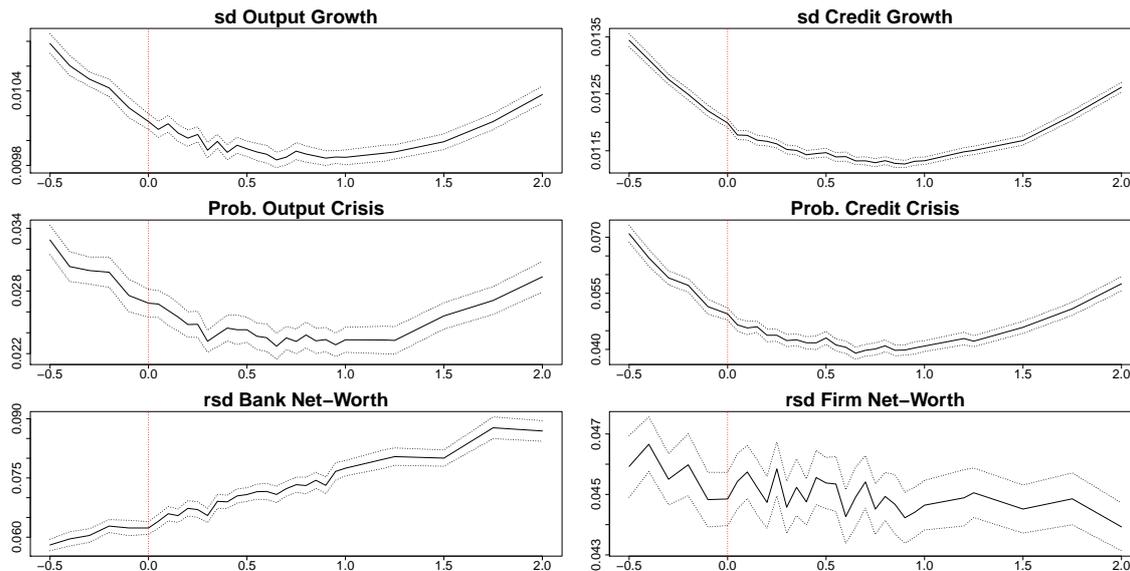


Figure 2: On the x-axis the values of the χ parameter, the solid line reports the average of one-hundred simulations and in dashed line the confidence interval of 95%. The dotted red line in correspondence with $\chi = 0$ where ‘de facto’ is applied the micro policy only. In the top left figure, the standard deviation of output growth rate. In the top right, the standard deviation of credit growth rate. In the center left panel, the output crisis probability. In the center right, the credit crisis probability. In the bottom left panel, the standard deviation of bank net-worth, measured as the aggregate standard deviation of equity divided by the average value. In the bottom right panel, the standard deviation of firm net-worth, measured as the aggregate standard deviation of equity divided by the average value.

192 Figure 2 shows that varying this sensitivity parameter (χ) has a U-shaped effect on the standard
 193 deviation of output and credit and on the probability of output and credit crisis. When χ is equal
 194 to zero the macro prudential policy is inactive reproducing ‘de facto’ the micro prudential policy.

195 Until $\chi = 0.8$, increasing χ reduces the volatility. Instead, for values above about 0.8, the
 196 volatility of output and credit increases.

197 However, the macro prudential policy seems to have a hidden side effect. Figure 2 shows
 198 that with higher values of (χ), the standard deviation of the bank net-worth increases, while the
 199 volatility of firm net worth does not change. Thus, the macro policy seems to shift part of the
 200 systemic risk to the banking sector. This is due to the fact that a fluctuating capital requirement
 201 impacts consistently on bank leverage and thus on bank profit volatility. Figure 3 shows that when
 202 the capital requirement ν_t is below the average bank leverage increases, because banks may offer a
 203 larger amount of credit at a lower interest rate (Equation 5), while the opposite occurs when ν_t is
 204 under the average level $\bar{\nu}$. In particular, with χ greater than zero, profits increase when the capital
 205 requirement is under the average but at the cost of higher profit volatility, due to the increased
 206 risk associated with higher leverage. On the other hand, when ν_t is over the average both the
 207 profit rate and its standard deviation decrease. According to Albertazzi and Gambacorta (2009)
 208 and De Haan and Poghosyan (2012), this excess of earnings volatility tends to lead to an unstable
 209 capital structure, augmenting financial instability. Therefore, a well calibrated macro prudential
 210 policy reduces the vulnerability of the economic systemic risk but at the potential cost of a more

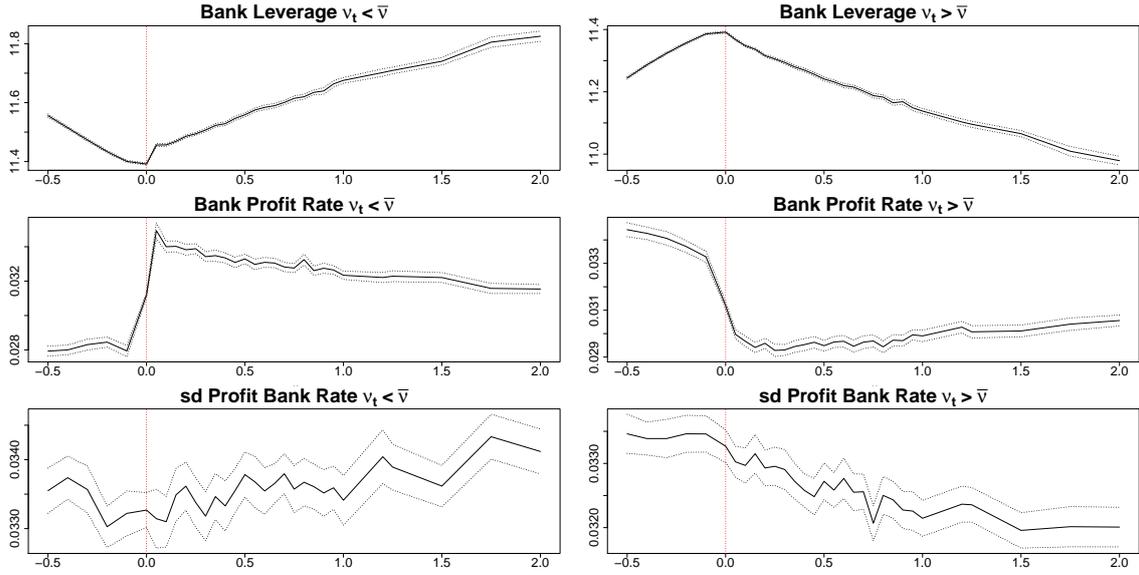


Figure 3: On the x-axis the values of the χ parameter, the solid line reports the average of one-hundred simulations and in dashed line the confidence interval of 95%. The dotted red line in correspondence with $\chi = 0$ where 'de facto' is applied the micro policy only. In the top left panel, the bank sector leverage, measured as aggregate credit divided by bank net-worth computed when the capital requirement is under the average ($\nu_t < \bar{\nu}$). In the top right, the bank sector leverage computed when the capital requirement is over the average ($\nu_t > \bar{\nu}$). In the center left, the profit rate when the capital requirement is under the average ($\nu_t < \bar{\nu}$). In the center right, the profit rate when the capital requirement is over the average ($\nu_t > \bar{\nu}$). In the bottom left, the standard deviation of the profit rate when the capital requirement is under the average ($\nu_t < \bar{\nu}$). In the bottom right, the standard deviation of the profit rate when the capital requirement is over the average ($\nu_t > \bar{\nu}$).

211 fragile banking system.

212

213 4 Simulation Results: Meso Prudential Policy

214 In this section we provide an alternative prudential scheme in which, in addition to the micro
 215 policy, the regulatory authority takes into account the number of banks-firms connections. We
 216 call this framework the meso prudential policy set-up because the evolving configuration of the
 217 connections on the credit market triggers the response of the financial stability authority.

218 Results show that a basic prudential policy that target just the more connected banks is able to
 219 reduce the vulnerability of the system without affecting negatively the banking sector as a whole.
 220 Indeed, increasing the capital requirement of the more connected bank reduces the possibility of
 221 diffusing local shocks, improving the resilience of the system.

222 In order to carry on our policy experiment, we define a simple measure of bank connectivity
 223 that allowed us to isolate an efficient prudential policy. The number connections of a bank b (NC_{bt})
 224 is given by the sum of the number of banks connected with the firms that received loans from the
 225 b bank. Thus, if NF_{bt} is the number of firms j connected with the bank b at time t and NB_{jt} is
 226 the number of banks that provide credit to a firm j at time t :

$$NC_{bt} = \sum_j^{NF_{bt}} NB_{jt}. \quad (26)$$

227 This measure tries to take into account both the direct links of a bank and the indirect con-
 228 nections between banks. Indeed, if a bank b provides credit to NF_{bt} firms and, in turn, these firms
 229 have not any other lender NB_{jt} is equal to one for each firm and $NC_{bt} = NF_{bt}$, thus NC_{bt} is equal
 230 to the number of direct links; while if these firms receive credit from other banks NB_{jt} becomes
 231 greater than one for each firm and NC_{bt} increases ($NC_{bt} > NF_{bt}$).

232 In this experiment, the meso prudential policy targets only banks that overcome a certain
 233 threshold level of connectivity (TC) increasing the capital requirement only for the more connected
 234 ones ($\nu_{bt} = \nu(1 + \delta_\nu)$), thus:

$$\nu_b = \begin{cases} \nu(1 + \delta_\nu) & \text{if } NC_{bt} > TC \\ \nu & \text{if } NC_{bt} \leq TC. \end{cases} \quad (27)$$

235 The top left panel of Figure 4 shows that increasing the link threshold (TC) reduces the
 236 number of banks targeted by the meso policy. The number of banks subject to the meso prudential
 237 regulation approaches to zero when the number of connections (NC_{bt}) is above 50. On the contrary,
 238 when the number of connections is too low, the sample of banks that should be monitored becomes
 239 high. For instance, when TC is equal to ten, the financial stability authority should monitor more
 240 than the eighty per cent of the banks of the model. The remaining panels of Figure 4 show that
 241 there is an intermediate interval of meso prudential intervention thresholds (TC) that stabilizes the
 242 economy in terms of probability of output crisis, output and credit growth volatility. For instance
 243 if the threshold is 40, even if the number of targeted banks is below 20% we observe a significant

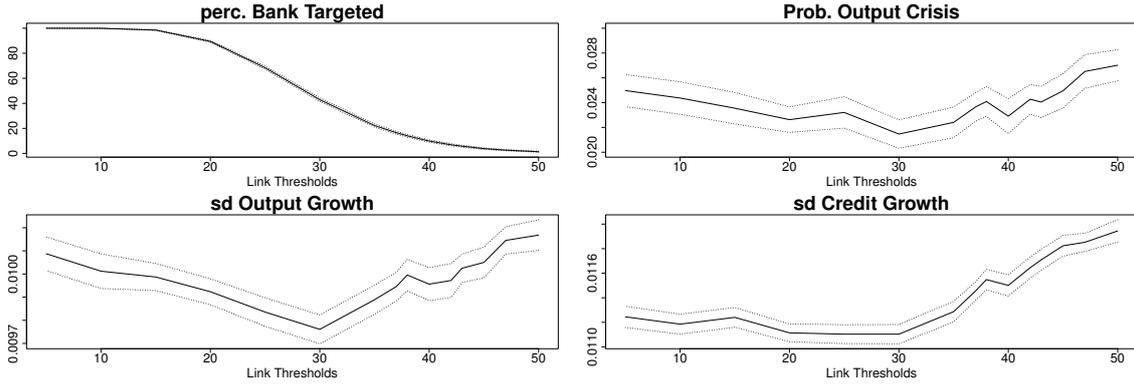


Figure 4: On the x-axis the values of the threshold level of connectivity. In the top left panel, the average number of bank targeted. In the top right, the output crisis probability. The bottom left, the output growth standard deviation. In the bottom right, the credit growth standard deviation.

244 reduction of the instability of the system with respect to the baseline scenario when only the micro
 245 prudential policy is applied.

246 The effectiveness of the meso prudential policy is related to the emerging topology of the credit
 247 network: the left panel of Figure 5 shows that bank connectivity distribution presents a fat tail
 248 log-normal distribution. As a consequence, just few banks can have a huge impact on the dynamics
 249 of the system and this justify the implementation of a meso prudential policy that target only the
 250 more connected ones, that potentially can diffuse local shocks across the entire network. However,
 251 also bank size presents a fat tail distribution (see the right panel of Figure 5).

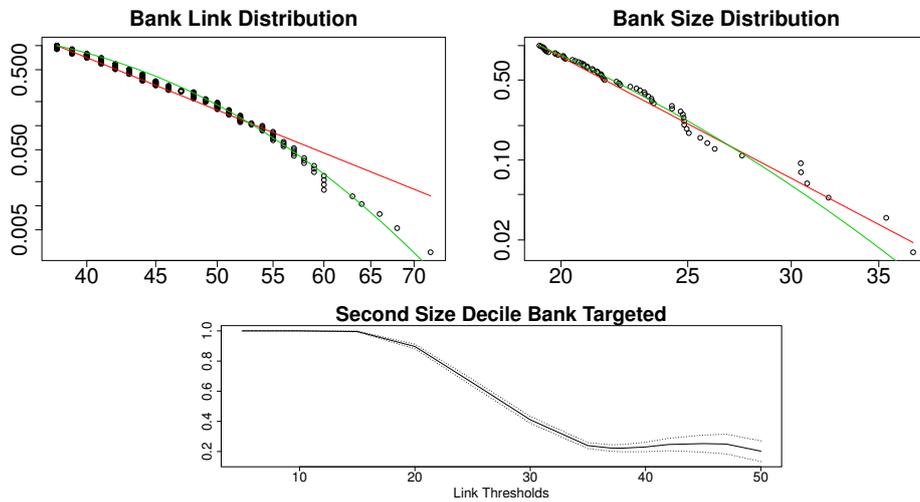


Figure 5: In the top left panel, the distribution of the connectivity measure used for the meso prudential policy. In the top right panel, the distribution of bank size, measured as the bank net-worth. In blue log normal distribution, in red Pareto distribution estimates. In the bottom panel, the percentage of banks belonging to the 20% of the larger ones that are targeted by the meso policy.

252 In fact, one of the possible critique to our experiment is that bigger banks in terms of size
 253 could be also the most connected banks of the credit network.¹ Nevertheless, according to our

¹The relationship between bank size and systemic risk is widely studied in the literature. See for instance Laeven

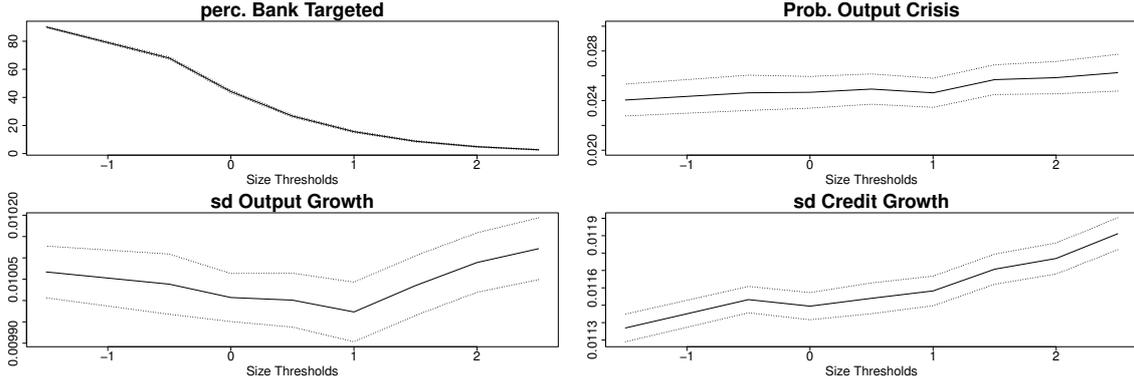


Figure 6: On the x-axis the values of the threshold level of size reported in standard deviations from the average. In the top left panel, the average number of bank targeted. In the top right, the output crisis probability. In the bottom left, the output growth standard deviation. In the bottom right, the credit growth standard deviation.

254 connectivity measure (Eq 26), the bottom panel of Figure 5 shows that more connected banks do
 255 not coincide with bigger ones. For instance, taking 40 as the meso policy threshold ($NC = 40$)
 256 and the second decile of the bank size distribution (thus bigger banks), only about the 20% of the
 257 banks belonging to this second decile are also the more connected ones.

258 Moreover, applying the same policy but using a threshold size instead of a measure of connec-
 259 tivity (increasing the capital requirement of the larger banks according to a given size threshold),
 260 we do not observe a significant impact on crisis probability even if volatility decreases in terms of
 261 output and credit standard deviations (Figure 6).

262 Moreover, we tested the effect of a combination of the meso prudential policy with the macro
 263 policy, thus letting change the capital requirement according to the credit cycle and at the same
 264 time targeting the more connected bank. ν_{bt} becomes:

$$\nu_{bt} = \begin{cases} \nu_t(1 + \delta_\nu) & \text{if } NC_{bt} > TC \\ \nu_t & \text{if } NC_{bt} \leq TC. \end{cases} \quad (28)$$

265 As shown in Figure 7, with respect to the baseline micro scenario, the combination of macro
 266 and meso policies has the better performance in reducing the volatility of the system. However,
 267 as for the macro policy scenario, it causes an increase of bank capital volatility. The meso policy
 268 stabilizes the economy, achieving comparable results in terms of output and credit volatility with
 269 respect to the macro policy. On the other hand, the meso prudential policy does not have a
 270 negative impact on bank capital volatility. In terms of policy recommendation the meso prudential
 271 policy seems to be a good compromise between the soundness of the banking system and a stable
 272 real economy.

et al. (2016, 2014).

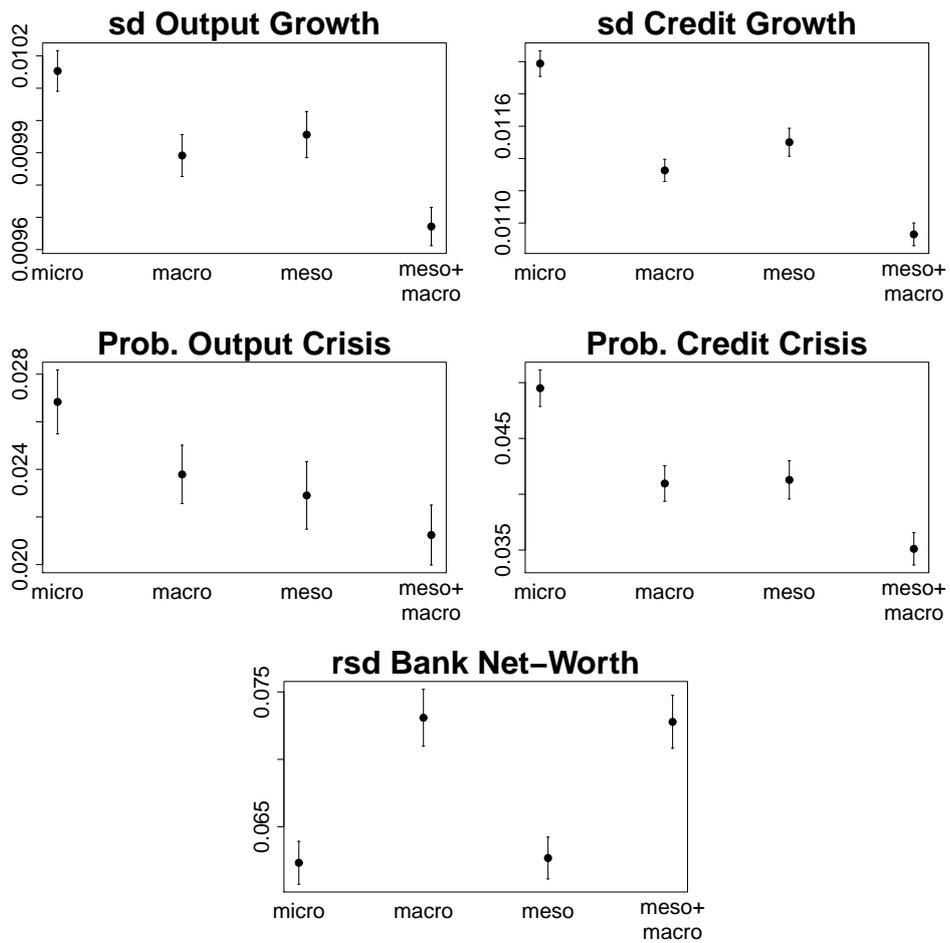


Figure 7: In the top left panel, the output growth standard deviation. In the top right, the credit growth standard deviation. In the center left, the output crisis probability. In the center right, the credit crisis probability. In the bottom, the standard deviation of bank net-worth.

273 5 Conclusions

274 The 2007/2008 crisis highlights the importance of regulation as a tool that may contribute to
275 improve the resilience of the economy. Our contribution tries to feed the literature that focus on
276 the interrelation between micro and macro prudential policy and the possible conflicts that may
277 arise among them. We also explore alternative regulatory frameworks.

278 In order to to that, we build an agent based credit network model. The ABM set-up allows
279 us to design policy measures that may target specific agents according to the interaction struc-
280 ture of the economy, taking into account in an unified framework both individual behaviors and
281 macroeconomic patters.

282 Simulation results show that combining micro and countercyclical macro prudential policy
283 reduces the volatility of the economic system. However, the dark side of this policy mix is an
284 increasing instability of the banking sector capital structure, in line with recent contributions by
285 Albertazzi and Gambacorta (2009) and De Haan and Poghosyan (2012).

286 Moreover, we propose a meso prudential policy rule based on the topology of the credit network,
287 in which the financial stability authority monitors the evolution of the connections among firms
288 and banks. Thus, we implement a combined micro and meso prudential policy that leads to higher
289 capital requirements only for more connected banks. In this way we reduce the diffusion of local
290 shocks to the whole economy without affecting the banking system. Our results show that a
291 combination of micro and meso prudential policy achieves the best compromise between banking
292 sector and real economy stability, according to the idea that financial institutions might not only
293 be "too big to fail", but they can also be "too interconnected or too systemic to fail" (see Markose
294 et al., 2012, Kelly et al., 2016, and Bongini et al., 2015).

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371 **Appendix A: Calibration**

Table 1: Calibrated parameters

parameters	Description	Value
M	Number of banks	100
N	Number of firms	1000
E_B^0	Initial Bank net-worth	1
E_F^0	Initial Firm net-worth	1
ϕ	Firm productivity	0.5
c	Firm variable cost	0.45
F	Firm fixed cost	0.01
r_d	Discount Rate	0.001
ζ	Bank maximum credit share	0.1
γ	Firms and banks dividend policy	0.5
\bar{v}	Capital requirement	0.09
ρ	Persistence of capital requirement adjustment	0.9
δ_ν	Meso policy capital requirement variation	0.15
δ	Capital and credit adjustment	0.1
κ	Capital requirement adjustment cost	10
β	Risk premium coefficient	1.25
\bar{r}	Risk free rate	0.005
η	Bank margin on the discount rate	10

372

373 We calibrated the model in order to reproduce realistic level of output volatility and aggregate
374 leverage, which are the crucial variables of our analysis. Considering the results of one-hundred
375 simulation of the baseline specification the output standard deviation is in line with data provide by
376 Uribe and Schmitt-Grohé (2017): data show that 1.12% is the word quarterly standard deviation
377 of output growth rates, while in simulation this value is close to 1.01%. Moreover, the credit over
378 output ratio is equal to 1.15, in line with the Euro area average between 2006 and 2015 that is
379 1.05. As expected credit volatility is higher than output volatility.

380 The number of agents depends on the necessity of a numerous population for producing robust
381 results during the simulation, the ratio between banks and firms follow Catullo et al. (2015) and
382 Catullo et al. (2017). The initial level of net-worth of firms and bank (E_b^0 and E_f^0) are fixed equal
383 to one for simplicity. The productivity of capital (ϕ) and the variable cost of capital (c) are fixed
384 in order to have a difference between productivity, thus expected revenues given $E(p) = 1$, and
385 variable costs that allow firms to borrow money until the quarterly interest rate is lower of 5%.
386 F is intended as little fixed cost that eliminates agents that are too small to impact on the credit
387 network, allowing new agent to enter. r_d is fixed to 0.001 for simplicity. ζ is 0.1 to avoid excessive
388 exposure of banks and, thus, an excessive failure rate of banks. γ is fixed to 0.5 for simplicity, value
389 of γ that are near to zero do not allow accumulation of firms and banks, on the other side value
390 of γ near to 1.0 lead to high levels of capital accumulation of firms, which generates an excessive
391 reduction of their leverage.

392 In the baseline scenario we keep the capital requirement fixed ($\nu = 0.09$ in line with Basel's
 393 Agreements, see Gerali et al., 2010), thus in this specification a basic micro prudential policy is
 394 implemented: banks have to align to the capital requirement in order to reduce their riskiness.
 395 Indeed, bank leverage is slightly above the maximum leverage possible for the banks given $\nu = 0.09$
 396 (Table 2) and the number of firms that receive loans is 13.51 a value larger than the ratio between
 397 the number of firms and banks. In this simple credit model the dynamic of credit and, thus, the
 398 probability of crisis occurrence depends on negative shocks affecting the economy through bad
 399 debts: debts that are not payed back by failing firms. The percentage of bad debt on credit is 1.9%
 400 with a low standard deviation, meaning that on average bad debt is quite stable through different
 401 simulations. Similarly $\bar{v} = 0.15$ allow an effective Meso policy. The remaining parameters are
 402 fixed in order to permit a good calibration of the model with respect to output standard deviation
 403 and aggregate leverage. In Appendix B, we report sensitivity experiments on the adjustment
 404 parameters δ and the parameters that are associated with the financial accelerator mechanism of
 405 banks ($\kappa, \beta, \bar{r}, \eta$) running one-hundred simulation for each specification. The sensitivity experiments
 406 are also implemented in the macro and meso scenarios.

407 Table 2 shows the emergent aggregate variable results in the micro baseline simulation.

	Micro (Baseline)		
Sd Output Growth Rate	1.01%	Prob Output Crisis	2.68%
	(0.003%)		(0.0692%)
Sd Credit Growth Rate	1.19%	Prob Credit Crisis	4.95%
	(0.004%)		(0.0840%)
rsd Bank Net-Worth	6.23%	rsd Firm Net-Worth	4.48%
	(0.0813%)		(0.0446%)
Credit/Output	1.15	Bank Leverage	11.41
	(0.0005)		(0.0017)
Average Bank Links	13.51	Bad-Debt/Credit	1.9%
	(0.0043)		(0.0001%)

Table 2: Macro Variable Simulated Results. Bank Leverage is measured as aggregate credit over aggregate bank net-worth. Average Bank Links are the average number of firms that receive loans from a bank. Bad-Debt/Credit is the value of the debts that are not payed back by failing firms divided by the total amount of credit in the economy.

408

409 **Appendix B: Sensitivity Analysis**

410 As expected reducing the adjustment parameter δ decreases the volatility of the system, while the
411 opposite happens when δ is increased. Also the parameters that impact on the financial accelerator
412 mechanism has been calibrated to produce realistic levels of systemic volatility $(\kappa, \beta, \bar{r}, \eta)$: values
413 that are too distant from the baseline tend to increase volatility. Indeed, for instance decreasing or
414 increasing too much the parameter β impacts in significant way on the system. When β is higher
415 than the benchmark level interest rate may easily surge when firm leverage augments, this may
416 increase rapidly firms's bad debt and, at the same time, may reduce the credit in the economy. On
417 the other hand, lower levels of β may increase too much firm capacity of borrowing money and,
418 thus leverage in the economy. Varying the other financial accelerator parameters produces similar
419 effects Moreover, the adjustment parameter (δ) and the parameters of the financial accelerator
420 seem to impact on the simulated system following the same patterns in both the Macro prudential
421 policy and the meso prudential policy specifications.

422

423

Table 3: Micro (Baseline) Configuration Sensitivity Analysis

variable	sd(Output)	sd(Credit)	prob(Crisis Output)	prob(Crisis Credit)	rsd(Bank net-worth)
Micro (Baseline)	1.015 (0.032)	1.199 (0.0405)	2.682 (0.6829)	4.95 (0.8333)	6 (0.8113)
δ					
0	0.897 (0.0265)	0.316 (0.1143)	1.14 (0.3913)	0.042 (0.0955)	15 (6.2339)
0.05	0.776 (0.0241)	0.603 (0.0251)	0.54 (0.3222)	0.06 (0.1119)	5 (0.6075)
0.15	1.374 (0.0516)	1.888 (0.0789)	7.568 (0.9393)	14.58 (1.4286)	8 (1.1505)
0.2	1.747 (0.062)	2.635 (0.094)	12.742 (1.233)	21.94 (1.3477)	9 (1.3007)
β					
0.75	1.203 (0.0356)	3.149 (0.1241)	5.028 (0.7995)	26.336 (1.4113)	25 (1.3228)
1	1.345 (0.0497)	2.521 (0.1196)	7.108 (1.02)	20.088 (1.4231)	14 (2.1747)
1.5	1.713 (0.0559)	1.705 (0.0571)	12.206 (1.2165)	12.08 (1.2355)	20 (1.0843)
1.75	1.607 (0.0502)	1.672 (0.0499)	10.604 (1.1364)	11.502 (1.2538)	20 (0.2484)
κ					
0	1.121 (0.0391)	1.553 (0.0702)	3.966 (0.7702)	10.02 (1.3826)	10 (1.4704)
5	1.049 (0.0399)	1.343 (0.051)	3.114 (0.8146)	6.986 (1.0595)	8 (1.1516)
15	1.377 (0.044)	1.88 (0.065)	7.672 (0.9183)	14.092 (1.1835)	5 (0.7352)
20	1.986 (0.0742)	3.109 (0.1226)	15.312 (1.3545)	24.398 (1.3383)	5 (0.6968)
\bar{r}					
0.003	1.316 (0.0448)	2.931 (0.1317)	6.758 (0.9906)	23.704 (1.553)	17 (1.5681)
0.004	1.192 (0.0384)	1.734 (0.0682)	4.924 (0.7805)	12.374 (1.3966)	9 (1.5062)
0.006	1.772 (0.056)	1.757 (0.0571)	13.014 (1.2303)	12.822 (1.2335)	5 (1.5292)
0.007	1.705 (0.0544)	1.707 (0.0531)	12.04 (1.1976)	12.098 (1.1287)	20 (0.4019)
η					
5	1.18 (0.0385)	1.718 (0.0713)	4.896 (0.8187)	12.278 (1.2713)	10 (1.6626)
7.5	1.102 (0.0364)	1.425 (0.0464)	3.788 (0.9038)	8.016 (1.0248)	8 (0.826)
12.5	0.939 (0.0336)	0.992 (0.0317)	1.798 (0.5857)	2.29 (0.6453)	6 (0.7992)
15	1.806 (0.0631)	1.785 (0.0621)	13.44 (1.2905)	12.94 (1.3164)	5 (1.3424)

Table 4: Macro Configuration Sensitivity Analysis

variable	sd(Output)	sd(Credit)	prob(Crisis Output)	prob(Crisis Credit)	rsd(Bank net-worth)
Macro	0.989 (0.0332)	1.132 (0.035)	2.378 (0.624)	4.098 (0.8028)	7 (1.0755)
δ					
0	0.895 (0.0328)	0.316 (0.1215)	1.096 (0.4561)	0.036 (0.0772)	13 (5.8194)
0.05	0.764 (0.026)	0.567 (0.0183)	0.58 (0.3321)	0.086 (0.1311)	6 (0.7924)
0.15	1.387 (0.0534)	1.907 (0.0775)	7.722 (1.0552)	14.76 (1.4176)	9 (1.3145)
0.2	1.919 (0.067)	3.017 (0.1266)	15.06 (1.2185)	25.21 (1.4423)	11 (1.6364)
β					
0.75	1.226 (0.0442)	3.08 (0.1053)	5.466 (0.9543)	24.976 (1.3613)	27 (2.4675)
1	1.31 (0.0484)	2.321 (0.0891)	6.576 (1.0388)	18.304 (1.5563)	18 (2.6735)
1.5	1.725 (0.0578)	1.714 (0.0599)	12.212 (1.1423)	12.262 (1.2169)	20 (1.0691)
1.75	1.608 (0.0504)	1.672 (0.0505)	10.614 (1.135)	11.498 (1.2619)	20 (0.2459)
κ					
0	1.079 (0.0349)	1.417 (0.0515)	3.542 (0.7766)	8.264 (1.0205)	11 (1.6437)
5	1.021 (0.0356)	1.26 (0.0412)	2.828 (0.7975)	5.866 (0.907)	9 (1.3323)
15	1.896 (0.1107)	2.903 (0.1942)	13.622 (1.5157)	22.228 (1.8315)	6 (0.8351)
20	7.242 (2.039)	77.252 (54.7402)	22.944 (7.9463)	39.58 (1.8896)	6 (2.0183)
\bar{r}					
0.003	1.291 (0.0466)	2.692 (0.1043)	6.532 (0.9599)	21.92 (1.3862)	20 (2.4957)
0.004	1.163 (0.037)	1.622 (0.0649)	4.544 (0.7811)	10.726 (1.26)	12 (1.7539)
0.006	1.781 (0.0519)	1.763 (0.0515)	13.064 (1.1082)	12.632 (1.24)	6 (1.3808)
0.007	1.705 (0.0538)	1.707 (0.0523)	12.042 (1.2431)	12.088 (1.1432)	20 (0.4099)
η					
5	1.154 (0.039)	1.618 (0.0596)	4.49 (0.7875)	10.852 (1.2096)	12 (1.6655)
7.5	1.064 (0.0362)	1.33 (0.043)	3.302 (0.8469)	6.924 (1.0397)	9 (1.1742)
12.5	0.911 (0.0343)	0.937 (0.034)	1.658 (0.5645)	1.786 (0.568)	6 (0.9157)
15	1.813 (0.0552)	1.791 (0.0556)	13.504 (1.1348)	13.156 (1.1643)	5 (1.3118)

Table 5: Meso Configuration Sensitivity Analysis

variable	sd(Output)	sd(Credit)	prob(Crisis Output)	prob(Crisis Credit)	rsd(Bank net-worth)
Meso	0.996 (0.0365)	1.151 (0.0443)	2.296 (0.72)	4.15 (0.8726)	6 (0.792)
δ					
0	0.893 (0.0344)	0.152 (0.1135)	1.15 (0.4959)	0.004 (0.0281)	11 (4.6958)
0.05	0.775 (0.0233)	0.599 (0.0232)	0.52 (0.2814)	0.08 (0.1421)	5 (0.7199)
0.15	1.295 (0.0349)	1.771 (0.0579)	6.252 (0.8573)	12.838 (1.2123)	7 (0.9714)
0.2	1.601 (0.0491)	2.409 (0.0845)	10.858 (1.2431)	20.206 (1.2363)	9 (1.1169)
β					
0.75	1.392 (0.0448)	3.366 (0.1068)	7.748 (1.0853)	27.488 (1.4189)	18 (1.5009)
1	1.255 (0.0443)	1.91 (0.0884)	5.552 (0.9203)	13.59 (1.4271)	12 (1.7305)
1.5	1.713 (0.0559)	1.705 (0.0571)	12.206 (1.2165)	12.08 (1.2355)	20 (1.0843)
1.75	1.607 (0.0502)	1.672 (0.0499)	10.604 (1.1364)	11.502 (1.2538)	20 (0.2484)
κ					
0	1.088 (0.0406)	1.509 (0.0679)	3.502 (0.7058)	9.262 (1.1833)	10 (1.41)
5	1.03 (0.0355)	1.309 (0.0498)	2.836 (0.659)	6.338 (0.9784)	8 (1.0059)
15	1.383 (0.0479)	1.913 (0.0743)	7.722 (1.03)	14.372 (1.2384)	5 (0.6419)
20	1.982 (0.0748)	3.112 (0.1229)	15.44 (1.3421)	24.544 (1.4383)	5 (0.6439)
\bar{r}					
0.003	1.334 (0.0471)	2.572 (0.1121)	6.916 (0.9901)	21.122 (1.36)	15 (2.2364)
0.004	1.133 (0.0327)	1.558 (0.0559)	4.008 (0.7445)	9.636 (1.1358)	9 (1.1235)
0.006	1.776 (0.0466)	1.76 (0.0479)	12.888 (1.1429)	12.626 (1.2009)	6 (1.6597)
0.007	1.705 (0.0544)	1.707 (0.0531)	12.04 (1.1976)	12.098 (1.1287)	20 (0.4019)
η					
5	1.122 (0.0362)	1.574 (0.0593)	3.956 (0.7689)	10.218 (1.2476)	9 (1.1604)
7.5	1.054 (0.0352)	1.327 (0.0453)	3.078 (0.7269)	6.718 (1.0131)	7 (0.8711)
12.5	0.934 (0.0317)	0.978 (0.0322)	1.754 (0.5825)	2.21 (0.5745)	6 (0.8278)
15	1.807 (0.0639)	1.789 (0.0634)	13.376 (1.3476)	13.02 (1.3149)	6 (1.3103)